



Course Syllabus

Course Code	Course Title	ECTS Credits
MATH-341	Numerical Analysis I	8
Prerequisites	Department	Semester
MATH-195, MATH-280 and one of COMP-111 or MATH-140	Computer Science	FALL
Type of Course	Field	Language of Instruction
Elective	Mathematics	English
Level of Course	Lecturer(s)	Year of Study
1 st Cycle	Nectarios Papanicolaou	3 rd
Mode of Delivery	Work Placement	Corequisites
Face-to-face	N/A	None

Course Objectives:

The main objectives of the course are to:

- Introduce students to the concepts of computational error, floating point arithmetic and asymptotic order.
- Cover in depth the theory and applications of numerical methods for solving nonlinear algebraic equations.
- Discuss direct methods for the solution of systems of linear equations in detail.
- Develop polynomial interpolation and numerical differentiation techniques.
- Introduce students to Numerical Quadrature.
- Discuss the implementation of numerical techniques using high-level programming Languages.

Learning Outcomes:

After completion of the course students are expected to be able to:

1. Use error and asymptotic order of convergence to assess numerical methods.
2. Implement approximation methods (Bisection, Newton, Secant etc) for finding the solution of nonlinear algebraic equations.
3. Apply direct methods to solve linear systems of algebraic equations.
4. Use Lagrange and Newton interpolation to approximate functions.

5. Utilize finite differences to approximate derivatives of functions.
6. Apply fundamental numerical integration methods (Trapezoidal rule, Simpson's and midpoint rules).
7. Design numerical algorithms and implement them using high-level programming languages.

Course Contents:

1. Review of Calculus and Introductory Concepts
 - a. Taylor's Theorem, the Mean Value and Extreme Value Theorems
 - b. Error and Asymptotic Order
 - c. Elementary Computer Arithmetic
2. Root Finding
 - a. The Bisection Method
 - b. Newton's Method
 - c. The Secant Method
 - d. Fixed Point Iterations
3. Numerical Solution of Linear Systems
 - a. Review of Linear Algebra
 - b. Gaussian Elimination and Pivoting
 - c. Operation Counts
 - d. LU Decomposition and the Thomas Algorithm.
4. Approximation of Functions
 - a. Lagrange Interpolation
 - b. Newton Divided Differences
 - c. Hermite Interpolation
 - d. Errors in Polynomial Interpolation
5. Numerical Differentiation
 - a. Finite Difference Approximations to Derivatives
 - b. Truncation Error
6. Numerical Integration
 - a. Review of the Riemann Integral
 - b. The Trapezoidal Rule
 - c. Simpson's Rule
 - d. The Midpoint Rule

Learning Activities and Teaching Methods:

Lectures, Homework and Programming Assignments.

Assessment Methods:

Homework, Mid-Term Exam, Programming Assignments, Final Exam.

Required Textbooks / Readings:

Title	Author(s)	Publisher	Year	ISBN
An Introduction to Numerical Methods and Analysis (2 nd Edition, also available as e-textbook)	J. F. Epperson	Wiley	2013	9781118367599

Recommended Textbooks / Readings:

Title	Author(s)	Publisher	Year	ISBN
Numerical Analysis (9 th edition)	R. L. Burden, and J. D. Faires	Brooks-Cole	2010	0538733519
Elementary Numerical Analysis (3 rd edition)	K. Atkinson, W. Han	Wiley	2004	0471433373