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| <b>Course Code</b><br>MATH-330E                 | <b>Course Title</b><br>Ordinary Differential Equations     | <b>ECTS Credits</b><br>7.5                  |
| <b>Department</b><br>Computer Science           | <b>Semester</b><br>Fall, Spring                            | <b>Prerequisites</b><br>MATH-191            |
| <b>Type of Course</b><br>Required/Elective      | <b>Field</b><br>Mathematics                                | <b>Language of Instruction</b><br>English   |
| <b>Level of Course</b><br>1 <sup>st</sup> Cycle | <b>Year of Study</b><br>2 <sup>nd</sup> or 3 <sup>rd</sup> | <b>Lecturer(s)</b><br>Dr Marios A. Christou |
| <b>Mode of Delivery</b><br>Face-to-face         | <b>Work Placement</b><br>N/A                               | <b>Co-requisites</b><br>None                |

### Objectives of the Course:

The main objectives of the course are to:

- Provide students with all the necessary techniques for solving first order ordinary differential equations.
- Familiarize students with the concepts of linear independence, fundamental solutions, general solutions and Initial Value Problems.
- Develop and demonstrate solution methods for linear higher order equations.
- Introduce students to applications and modelling using Ordinary Differential Equations.
- Provide students with the fundamentals of the power series method
- Introduce students to the Laplace Transform and its applications

### Learning Outcomes:

After completing the course students are expected to be able to:

1. Apply a number of techniques for solving 1<sup>st</sup> order equations
2. Construct models and analyze simple problems using 1<sup>st</sup> order equations
3. Compute the solutions of higher order linear equations with constant coefficients
4. Apply the power series method for solving 2<sup>nd</sup> order linear equations with variable coefficients
5. Implement the Laplace Integral Transform and use its properties to solve linear initial value problems

### Course Contents:

1. First Order Differential Equations-Initial Value Problems
  - Linear Equations
  - Separable Equations

- Integrating Factors
  - Exact Equations
  - Applications: Mixing and Compound Interest
2. Second Order Equations
    - Equations with Constant Coefficients,
    - Non-Homogeneous Equations,
    - Linear Independence and the Wronskian,
    - Applications: Springs and Electric Circuits
  3. Higher Order Equations with Constant Coefficients
    - Higher Order Initial-Value Problems
    - The Wronskian for Higher Order Equations
    - The method of Undetermined Coefficients
  4. Power Series Solutions of Second Order Equations with Variable Coefficients
    - Regular points
    - Regular and irregular singular points
    - Series solutions near a regular point
  5. Euler Equations
  6. The Laplace Transform Method for Solving Initial Value Problems
    - Definition of the Laplace Transform
    - Laplace Transforms of basic functions
    - Solving Initial Value Problems (IVPs) with Laplace transforms
    - IVPs with step functions and discontinuous forcing functions
    - IVPs with impulse functions and the Dirac delta function
  7. Systems of Ordinary Differential Equations

#### **Learning Activities and Teaching Methods:**

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| Lectures, Handouts and Assignments |
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#### **Assessment Methods:**

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| 2 Mid-Term Exams; Final Exam; Class Participation. |
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#### **Required Textbooks/Reading:**

| Authors           | Title   | Publisher | Year | ISBN          |
|-------------------|---|-----------|------|---------------|
| Boyce and DiPrima | Elementary Differential Equations and Boundary Value Problems | Wiley     | 2005 | 0-471-43338-1 |

#### **Recommended Textbooks/Reading:**

| Authors          | Title  | Publisher | Year | ISBN          |
|------------------|--|-----------|------|---------------|
| E. A. Coddington | An Introduction to Ordinary Differential Equations | Dover     | 1989 | 0-486-65942-9 |